

Connection between DIS at small x and high energy pp collisions

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hh-coll.: Conventional collinear factoriz.

→ High $p_{\perp}$ jets

But: Minijet cross section diverges

$$\sigma_{\text{jet}} \sim \frac{1}{p_{\perp}^4}$$

Also total $E_{\perp}$ diverges.

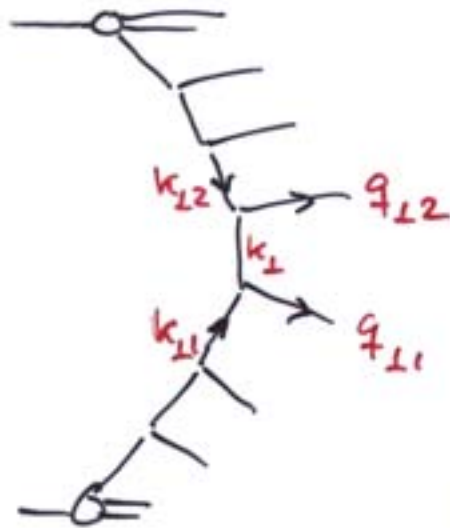
Cut off needed: Pythia fit to data $\Rightarrow$

$\Rightarrow p_{\perp 0} \sim 2 \text{ GeV}$ growing with energy.

Difficult to extrapolate to the
high energies at LHC.

$k_{\perp}$ -factorization

cf. talk by Szechurek



$$k_{\perp} < k_{\perp 1}, k_{\perp 2} \Rightarrow$$

Off shell $M\bar{E}$ does
not blow up when

$$k_{\perp} \rightarrow 0.$$

$k_{\perp}$ does not determine

$$\frac{\text{jet } q_{\perp}}{\text{total } E_{\perp}} \text{ finite}$$

$\mathcal{O}_{\text{jet}} > \mathcal{O}_{\text{tot}} \Rightarrow$ Several hard subcollisions
in each event.

$\Rightarrow$ correlations important

Pedestal effect $\Rightarrow$ hard coll. not indep

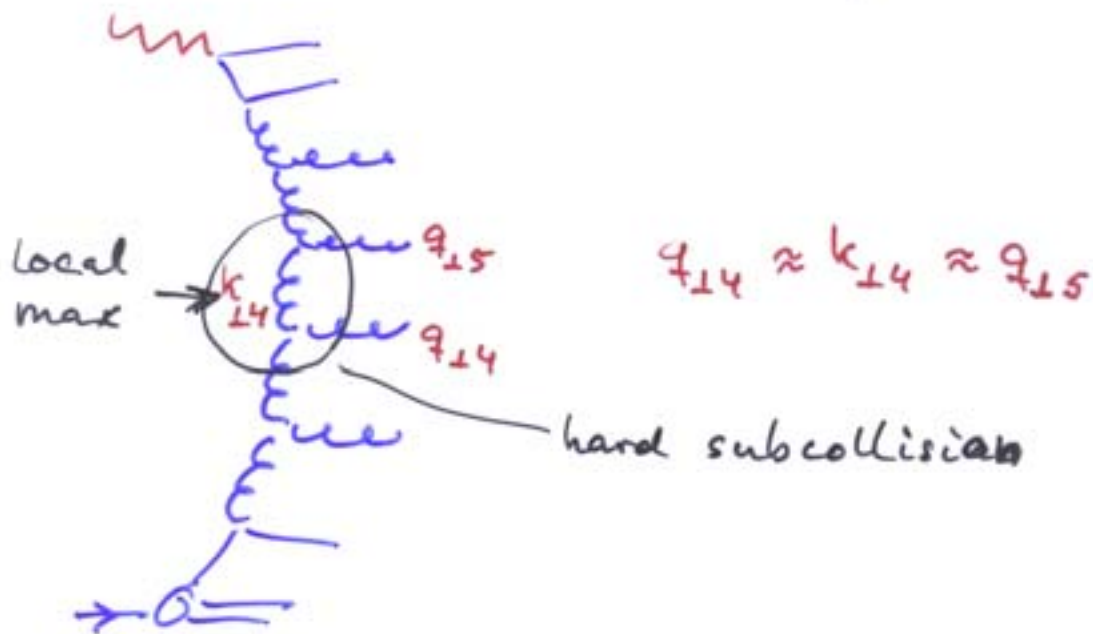
Impact parameter dependence:

central coll.: many minijets

peripheral coll.: few " ~

How can DIS data improve predictions for hadronic collisions?

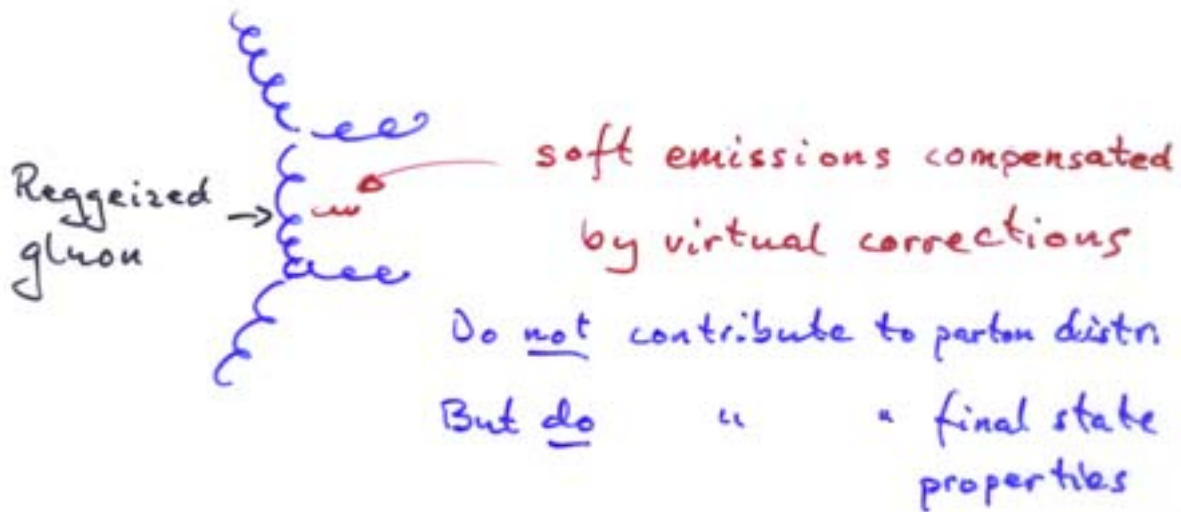
Small x ; BFKL: Non- k_T -ordered parton chains important



Single local max $\rightarrow$ Resolved photon interaction.

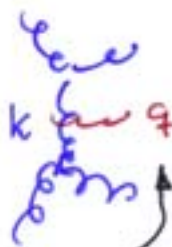
Several local maxima $\Rightarrow$
Correlated hard subcoll.

BFKL integral eq. only inclusive



Added with Sudakov form factors.

CCFM-model interpolates between BFKL & DGLAP



Some soft emissions included in initial state rad. $\Rightarrow$

Extra suppression from non-eikonal form factors

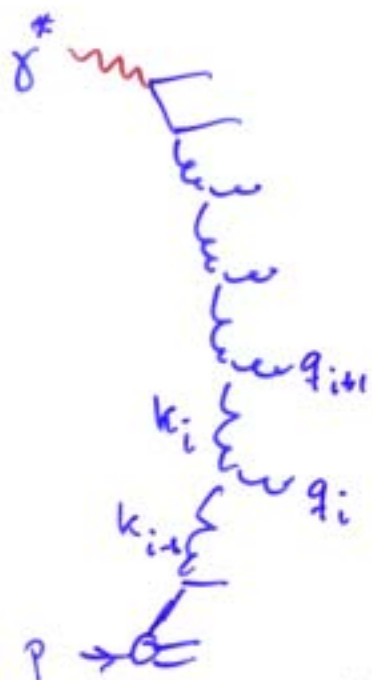
Linked Dipole Chain (LDC) model (Lund)

Reformulation and generaliz. of CCFM

Separation ISR - FSR more similar to BFKL formal

q final state if $q_{\perp} < k_{\perp}$

$\Rightarrow$ ISR chain in LDC is symmetric
photon end — proton end.



Leading order in $\ln 1/x$:

$$F \sim \sum_n \prod_i^n \iint \frac{3\alpha_s}{\pi} \frac{dz_i}{z_i} \frac{dq_{\perp i}^2}{q_{\perp i}^2} \times \theta(q_{\perp i} - \min(k_{\perp i}, k_{\perp i-1}))$$

$$q_{\perp i}^2 \approx \max(k_{\perp i}^2, k_{\perp i-1}^2)$$

$$\Rightarrow \frac{dq_{\perp i}^2}{q_{\perp i}^2} \approx \frac{dk_{\perp i}^2}{k_{\perp i}^2} \quad \text{except local max. or min.}$$

$$\text{local max. } k_{\perp i} \Rightarrow \frac{dk_{\perp i}^2}{k_{\perp i}^4} \quad \text{hard subcoll.}$$

$$\text{local min } k_{\perp i} \Rightarrow dk_{\perp i}^2 \quad \text{no divergence}$$

(fig.)

Symmetry $\Rightarrow$ Also applicable to hh coll.

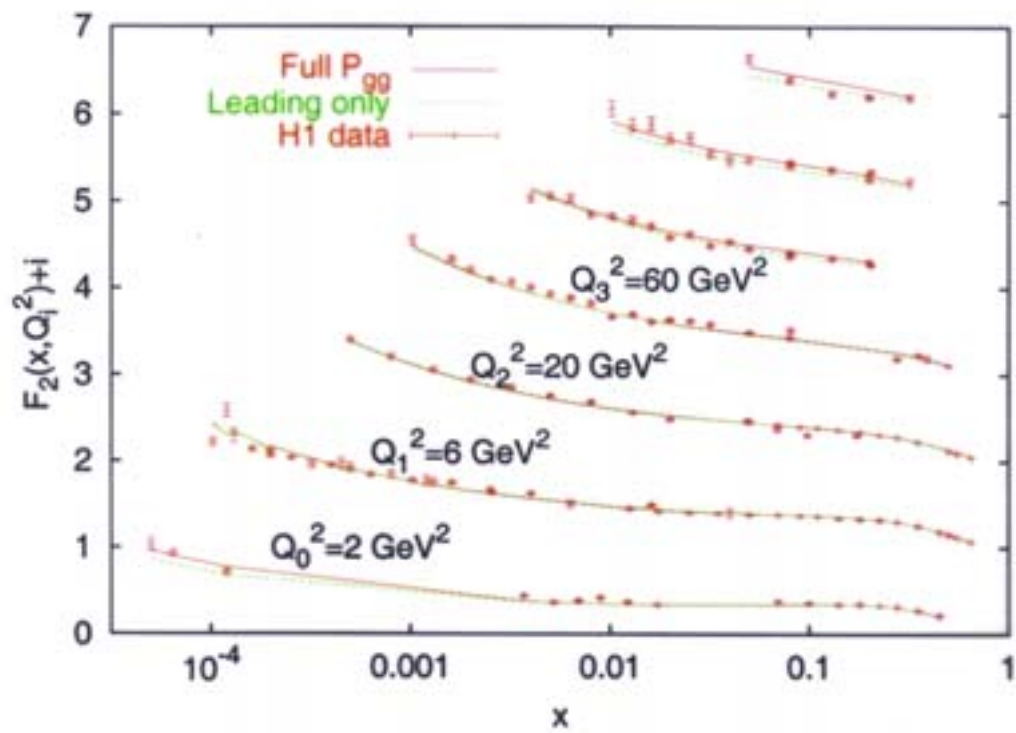
Fit to DIS $\Rightarrow$ cross section for

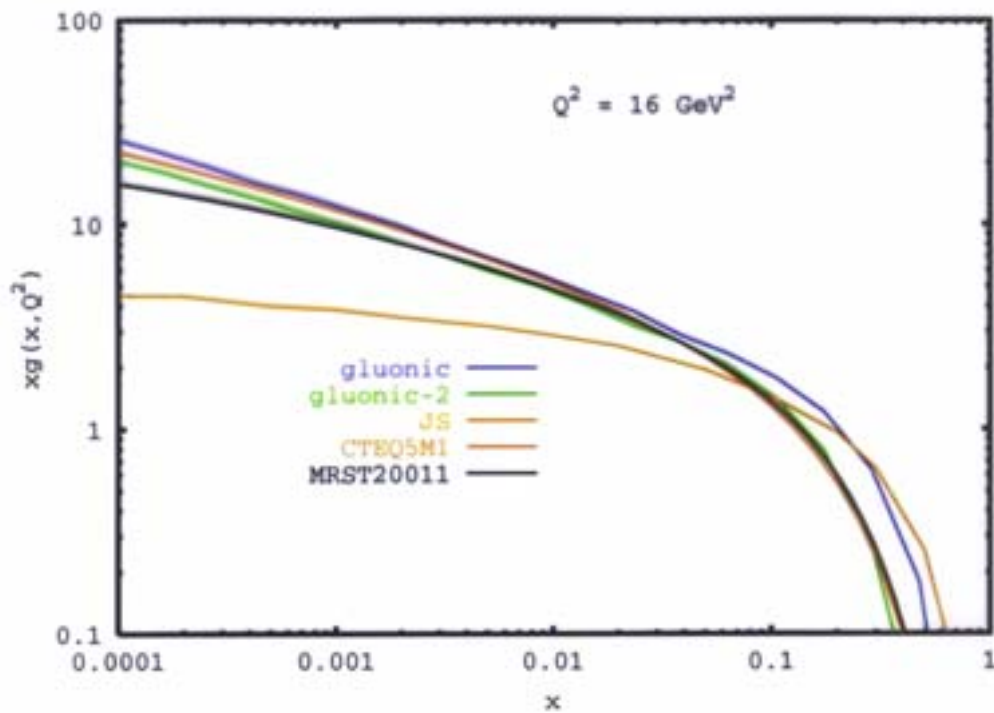
a chain in pp coll.

(possibly more than one hard subcoll.)

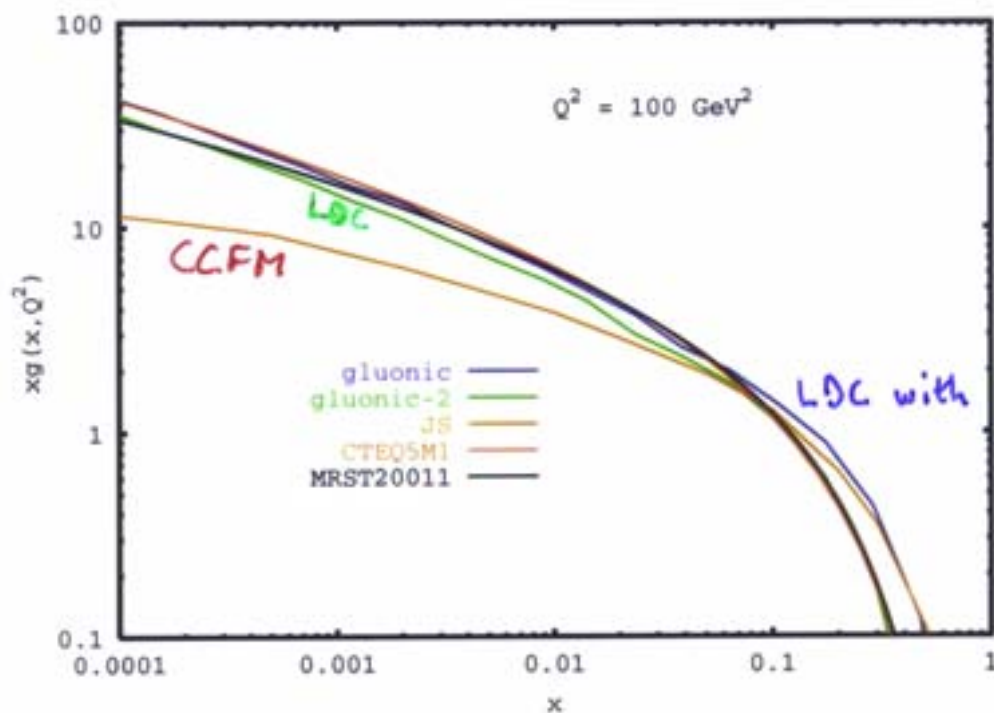
F_2

Linked Dipole Chain MC





Integrated gluon distributions



Lönnblad-Miu - GG JHEP '02

Potential problem

Fit to DIS : Running $\alpha_s \Rightarrow$

$\Rightarrow$ Soft cutoff Q_0 needed.

Good fits to DIS data possible with different cuts if input distrib. $f_0(x, Q_0^2)$ is adjusted accordingly.

??



hard chain
 $q_1 > Q_0$



soft chain
 $q_1 < Q_0$

$Q_0^2 \nearrow \Rightarrow \searrow$



Linked Dipole Chain model for hadronic coll.

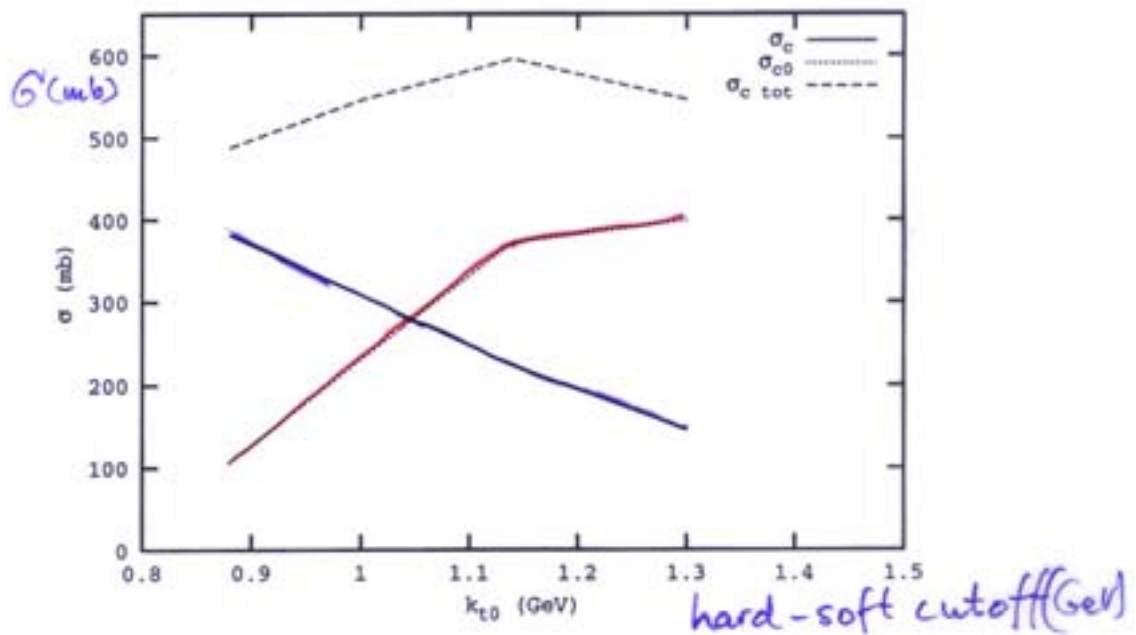
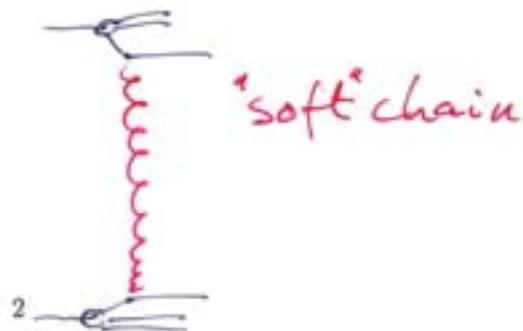


Figure 2: The cross section per chain in the LDC model as a function of the cutoff, k_{t0}^2 . The full line is the cross section for chains with at least one emission above the cutoff, the dotted line is for chains without emissions above the cutoff, and the dashed line is the sum of the two. Note that the input parton densities have been refitted for each value of k_{t0}^2 .

Cross section for hard scatt chain



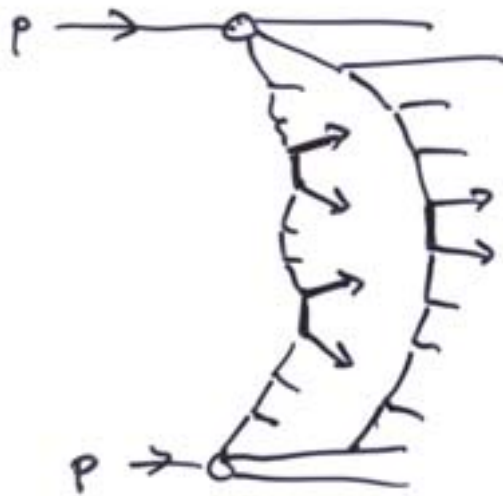
Total cross section for a chain
independent of the soft cutoff !!

$$\sigma_{\text{chain}} = \sigma_{\text{hard chain}} + \sigma_{\text{soft chain}}$$

fixed from DIS

Strong connection DIS - pp scatt.

Multiple interactions from 2 hard scatterings in the same chain and from more than one chain in a single event



Uncorrelated chains : Poisson distrib.

Pythia : b-dep. double Gaussian $\sim$ Geometric distrib.

but tail reduced by
energy conserv.

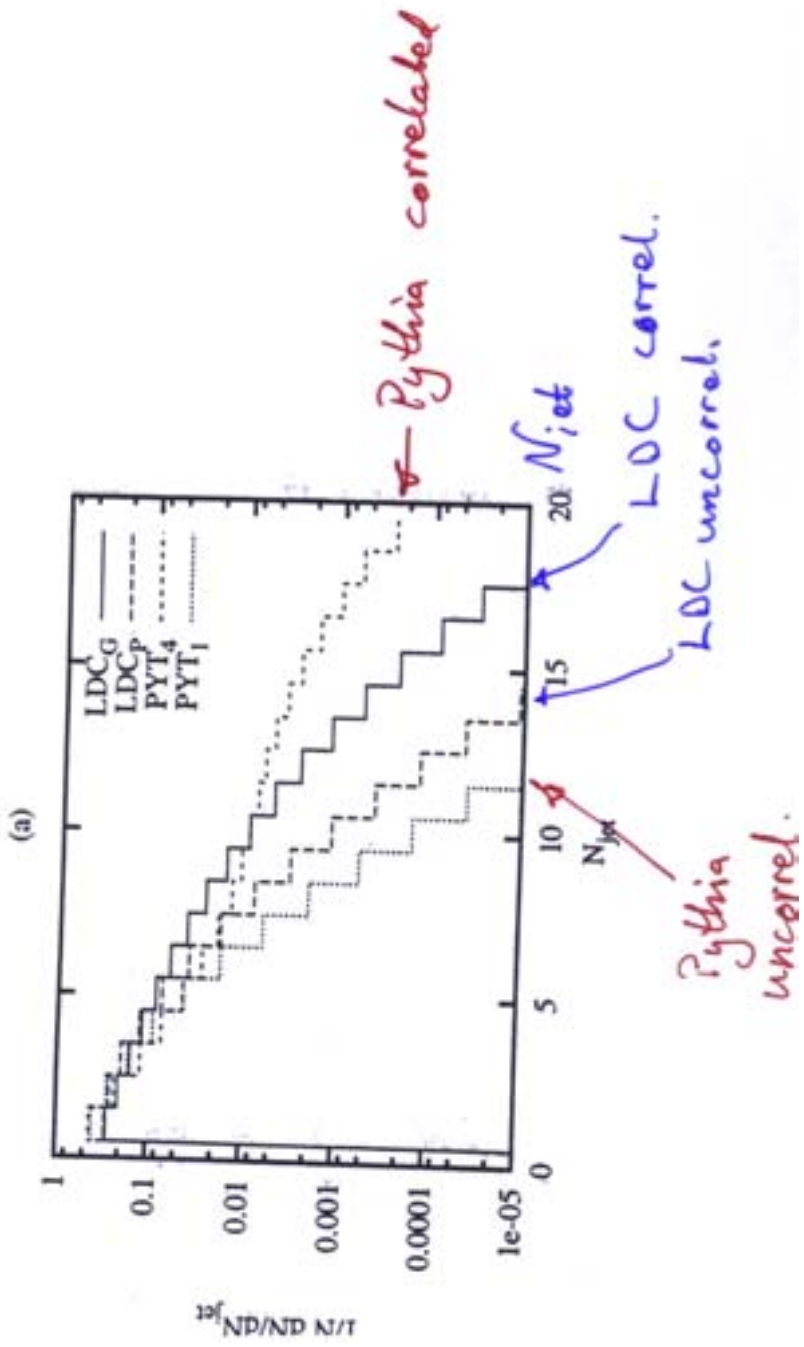
$$(\langle n_{ch} \rangle \sim 14 \rightarrow \sim 7)$$

Prel. results, Hadroniz. not included

(dep. on colour connection)

$$\sqrt{s} = 1.8 \text{ TeV}$$

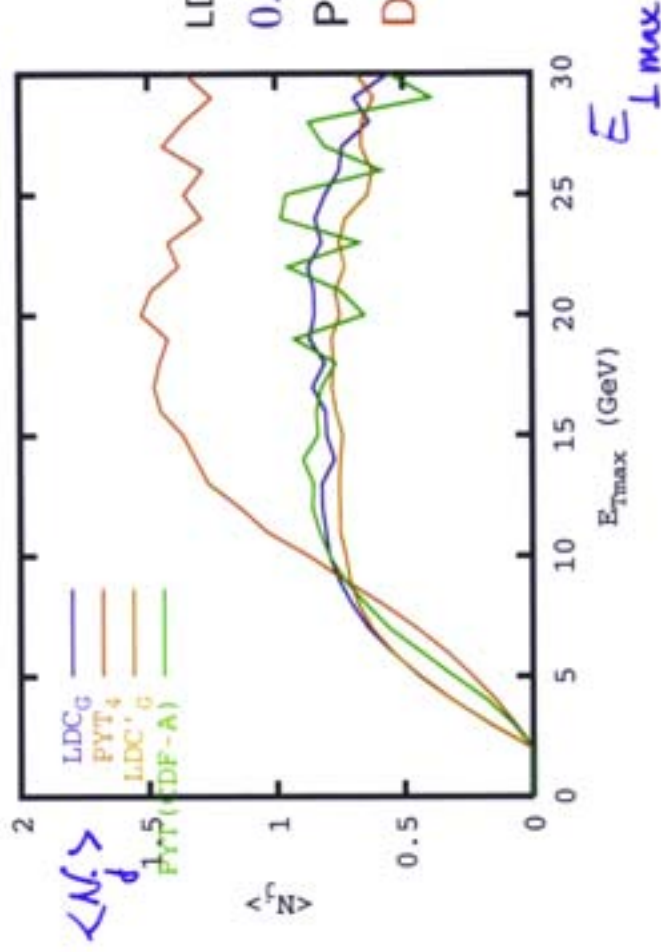
minijets in $|\eta| < 2.5$ in events with $E_{T, \text{max}} > 10 \text{ GeV}$



Cutoff dependence

Pedestal effect: $k_{\perp}$ jets in minimum azim.

1.8 TeV ($\eta < 2.5$)



LDCMC $k_{\perp 0}$:

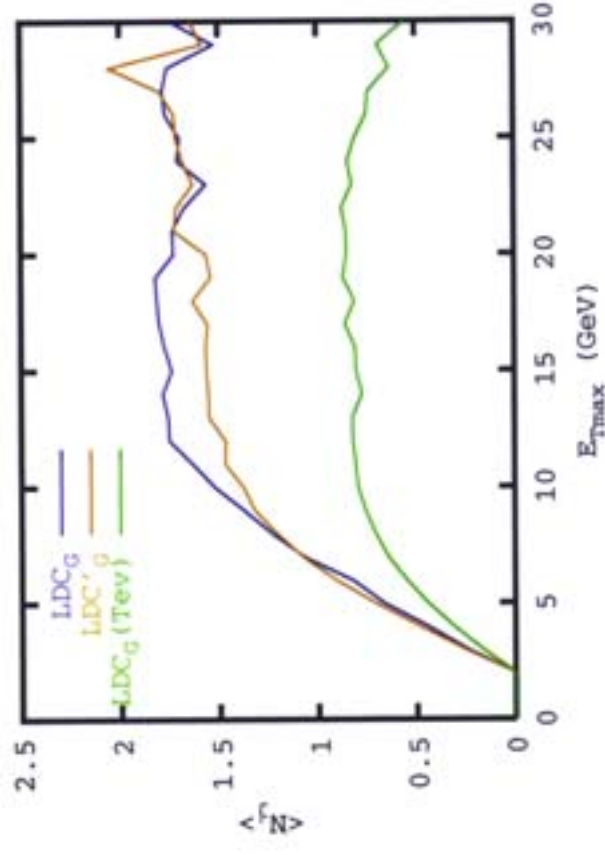
0.99 GeV $\rightarrow$ 1.3 GeV

PYTHIA:

Default $\rightarrow$ CDF-A $\uparrow$ CDF tune

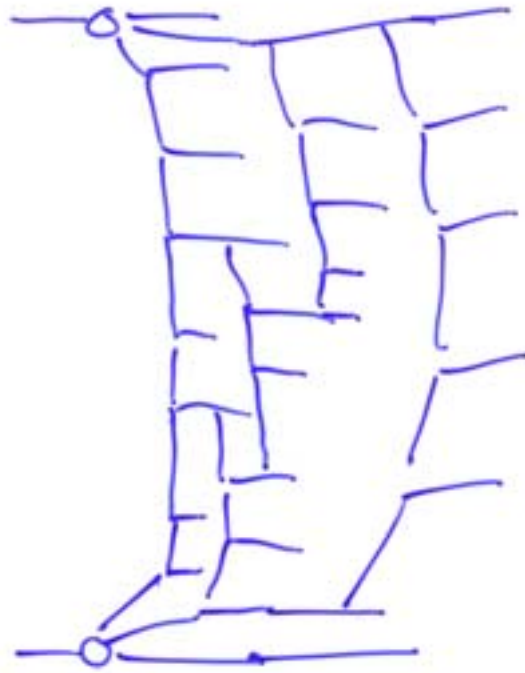


LHC?



LDCMC $k_{\perp 0}$:
 $0.99 \rightarrow 1.3$ GeV

Unitarization and saturation



$$\mathcal{G}_{\text{chain}} \propto s^\lambda$$

$$\langle n_{\text{chain}} \rangle \propto \frac{s^\lambda}{\mathcal{G}_{\text{tot}}}$$

The chains join at one end at the same rate as they multiply at the other.

Work on saturation and diffraction
in progress.

Conclusions

- New way of describing final states
in hadronic collisions
uses $k_{\perp}$ -factorization (LDC)
- Cutoff independent underlying event
and pedestal effect
- Everything predicted from fit to
DIS F_2

Future:

- Colour connections between mult. chains
must be improved
- Studies of correlations, saturation
and diffraction in progress